# Assimilating Spatially Dense Data for Subsurface Applications—Balancing Information and Degrees of Freedom

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# Two Porous Media

with different fluid conductivity (permeability)





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Sandstone sample

Sponge

# Two Porous Media

with different fluid conductivity (permeability)





Sandstone sample

Sponge

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#### Task: estimate permeability, k(x)

### Seismic Data



Offshore seismic data acquisition

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### Seismic Data



Offshore seismic data acquisition

#### Seismic data are spatially dense

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### Seismic Data



Offshore seismic data acquisition

#### Seismic data are spatially dense

Link between seismic data and k(x)?

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 $k(x) \rightarrow$  flow modeling  $\rightarrow$  fluid pressure and fluid content

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F. pressure and f. content  $\rightarrow$  petro-elastic modeling  $\rightarrow$  elastic properties

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Elastic properties  $\rightarrow$  seismic modeling  $\rightarrow$  simulated seismic data

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F. pressure and f. content  $\rightarrow$  petro-elastic modeling  $\rightarrow$  elastic properties

Elastic properties  $\rightarrow$  seismic modeling  $\rightarrow$  simulated seismic data

We use elastic properties ('inverted seismic data') as 'seismic data' when estimating k(x)

### Background

Inverted seismic data

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#### Background Inverted seismic data

#### Elastic properties: $V_p$ , $V_s$ , $\rho$ , ... are pixel fields

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Spatially dense  $\rightarrow$  high potential for estimating k(x)

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Some information will, however, be lost

### Background

Ensemble-based methods



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### Background Ensemble-based methods

Degrees of freedom (DOF) is limited by ensemble size, E (assuming no localization)

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Feature extraction may alleviate this problem

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Subspace pseudo inversion is another alternative

# Background

Balancing information and DOF

### Background Balancing information and DOF

Both feature extraction and subspace pseudo inversion reduce data influence

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### Background Balancing information and DOF

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Hence, some of the information available is not applied in the data assimilation

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### Background Balancing information and DOF

Both feature extraction and subspace pseudo inversion reduce data influence

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Need to balance the applied information content against available DOF

# Scope

Balancing information and DOF

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### Scope Balancing information and DOF

How to reduce data influence sufficiently to avoid unwarranted strong uncertainty reduction without discarding important information?

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### Scope Balancing information and DOF

How to reduce data influence sufficiently to avoid unwarranted strong uncertainty reduction without discarding important information?

Alternatively:

How to increase ensemble size sufficiently to handle spatially dense data without increasing computational cost?

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Approaches

Approaches

Data coarsening



Approaches

Data coarsening

Structure extraction

Approaches

Data coarsening

Structure extraction

Subspace pseudo inversion

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# Reduce Data Influence-Approaches

Data coarsening



Data field 400 data

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# Reduce Data Influence-Approaches

Data coarsening



Data field 400 data



Coarsened data field 49 data

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#### Structure extraction



Data field 400 data

#### Structure extraction



Data field 400 data



Smoothened field with 60 data

#### Structure extraction









#### Structure data: point locations

Subspace psudo inversion<sup>1</sup>

Subspace psudo inversion<sup>1</sup>

Matrix to be inverted in Kalman gain,  $W = SS^T + (E - 1)C_D$ , may be (numerically) singular

<sup>1</sup>Evensen G, Data Assimilation; the Ensemble Kalman Eilter  $\mathbb{P} \to \mathbb{C} = \mathbb{P} \oplus \mathbb{C}$ 

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Use pseudo inverse,  $W^+$ , but this is costly for large no. of data

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Subspace psudo inversion<sup>1</sup>

Matrix to be inverted in Kalman gain,  $W = SS^T + (E - 1)C_D$ , may be (numerically) singular

Use pseudo inverse,  $W^+$ , but this is costly for large no. of data

Approximate W by  $B = SS^T + (E - 1)SS^+C_D(SS^+)^T$ , and use  $B^+$  in Kalman gain

<sup>&</sup>lt;sup>1</sup>Evensen G, Data Assimilation; the Ensemble Kalman Eilter 🕬 🚛 Kalman Eilter

# Increase ensemble size without increasing cost

Approach–Upscaled simulations<sup>2</sup>

Standard forward model:  $k(x) \rightarrow f(k(x))$ 

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Upscaled forward model:  $k(x) \rightarrow u(k(x)) \rightarrow f(u(k(x)))$ 

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Computational cost ~ solving linear system ~  $\mathcal{O}(G^{\beta})$ ;  $\beta \in (1.25, 1.5)$ 

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Computational cost  $\sim$  solving linear system  $\sim \mathcal{O}(G^{\beta})$ ;  $\beta \in (1.25, 1.5)$ 

Ensemble computational cost 
$$\sim G^{\beta}E = G_{u}^{\beta}E_{u} \Rightarrow E_{u} = \left(rac{G}{G_{u}}
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Ensemble computational cost 
$$\sim G^{\beta}E = G_{u}^{\beta}E_{u} \Rightarrow E_{u} = \left(\frac{G}{G_{u}}\right)^{\beta}E$$

Cost of  $E_u$  upscaled simulations equals that of E standard simulations

### Examples Setup

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#### Original data: bulk-velocity $(V_p)$ pixel field

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Notation for labelling plots:



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*True*: results obtained with pixel data and E = 4800

Original data: bulk-velocity  $(V_p)$  pixel field

Notation for labelling plots:

*True*: results obtained with pixel data and E = 4800

*Estimate*: results obtained with any type of data and computational cost corresponding to E = 100 standard simulations

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### Examples Pixel data



$$t = t_1$$



$$t = t_3$$



$$t = t_2$$



 $t = t_4$ 

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k(x) estimate with pixel data on 20x20 grid



True mean



True stdv

k(x) estimate with pixel data on 20x20 grid



True mean



True stdv



Estimate mean



Estimate stdv

#### k(x) estimate with data coarsening to 7×7 grid



True mean



True stdv



Estimate mean



Estimate stdv

k(x) estimate with 98% energy subspace pseudo inversion



True mean



True stdv



Estimate mean



Estimate stdv

#### k(x) estimate with 10×10 upscaled simulations



True mean



True stdv



Estimate mean



Estimate stdv

#### Coarser simulation grid

<i>d</i> <sub>3</sub>	$d_4$
$d_1$	$d_2$

Data-grid detail



#### Simulation-grid detail

#### Coarser simulation grid

<i>d</i> <sub>3</sub>	$d_4$
$d_1$	$d_2$

Data-grid detail

5	S
5	5

Simulation-grid detail after downscaling to data grid

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<i>d</i> <sub>3</sub>	$d_4$
$d_1$	$d_2$

Data-grid detail

5	5
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Simulation-grid detail after downscaling to data grid

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s cannot match four different values

#### Coarser simulation grid

d <sub>3</sub>	$d_4$
$d_1$	$d_2$

Data-grid detail

5	s
5	5

Simulation-grid detail after downscaling to data grid

s cannot match four different values

Not a problem with upscaled simulations and well data

k(x) estimate with 10×10 upscaled simulations and 10×10 data coarsening



True mean



True stdv



Estimate mean



Estimate stdv



Investigated how to balance information against available DOF

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Three ways of reduction of data-space influence (data coarsening, structure extraction, subspace pseudo inversion) and one way of increasing ensemble size without increasing cost (upscaled simulations) have been considered

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Upscaled simulations combined with data coarsening gave good results, particularly when scales of simulation grid and data grid were similar

## Acknowledgements

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